

Free Core Nutation period inferred from tidal gravity measurements at Józefosław, Poland

Quality factor

Q factor estimation with Bayesian method

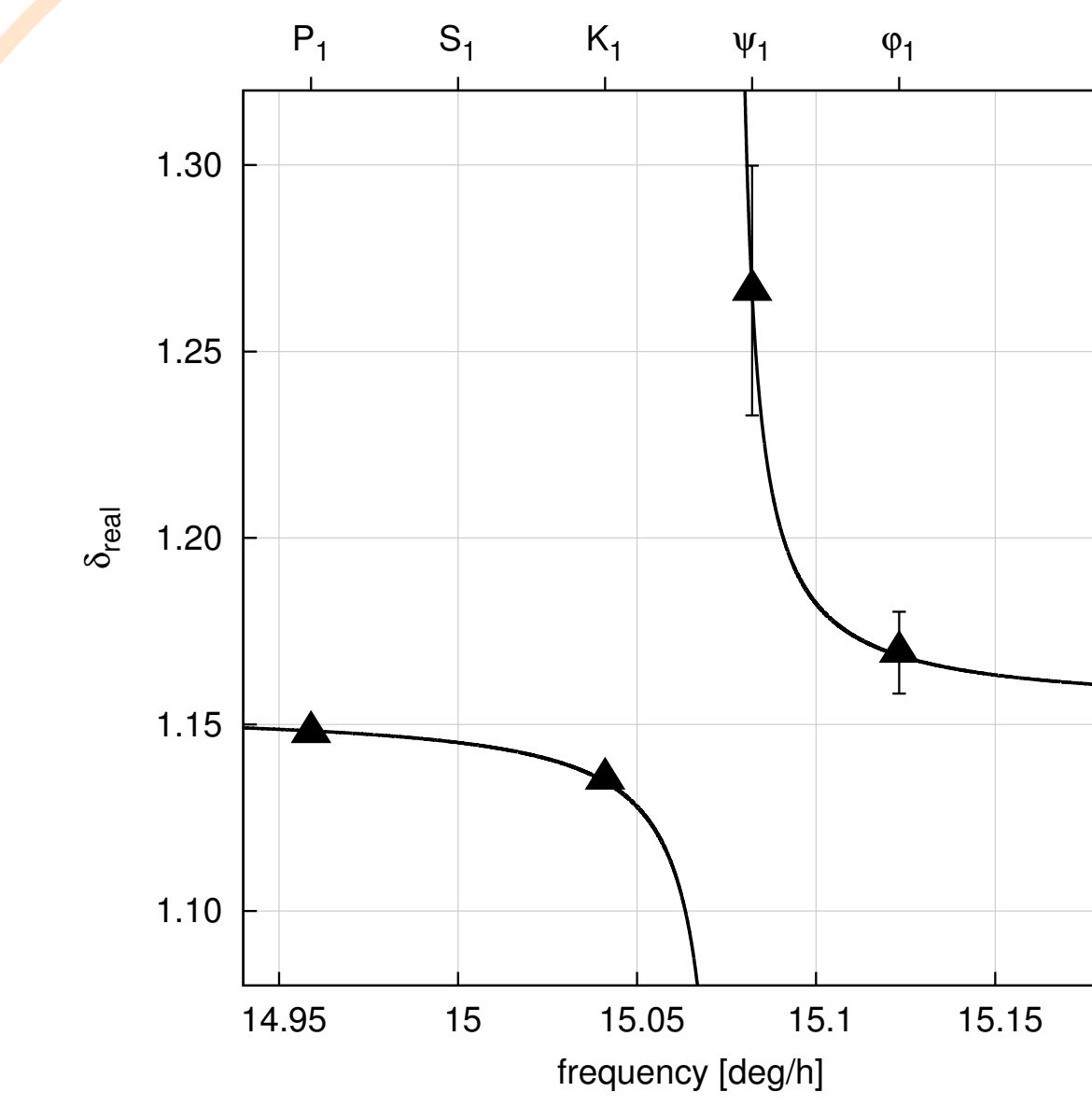
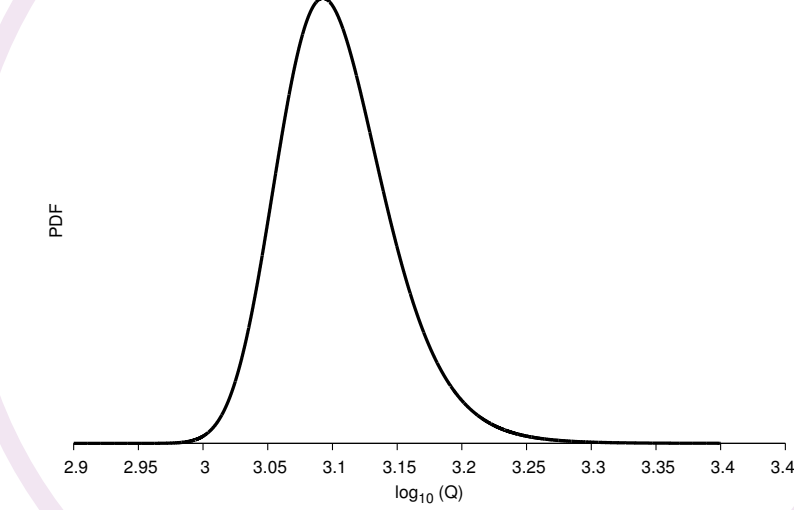


Figure: Resonance curve fitted to gravimetric factors

Table: Comparison of FCN period determination using different strategies

Solution	T [SD]					A. [10^4 h-deg $^{-1}$]				
	M_2	ν_2	K_1	ν_1	A_1	M_2	ν_2	K_1	ν_1	A_1
NC	408.3	(396.5 - 420.9)	5.47	(±0.20)	412.0	(391.5 - 434.7)	5.40	(±0.32)		
PC	413.2	(402.0 - 425.0)	5.45	(±0.17)	418.0	(397.1 - 441.3)	5.37	(±0.31)		
OTLC	423.2	(407.0 - 440.7)	6.87	(±0.30)	423.4	(407.5 - 436.3)	6.90	(±0.27)		
PC+OTLC	430.2	(421.4 - 439.5)	6.80	(±0.15)	426.0	(414.1 - 438.6)	6.88	(±0.21)		
Solution	K_1, ν_1, ν_2									
NC	408.5	(401.7 - 415.5)	5.47	(±0.11)	412.3	(385.8 - 442.6)	5.39	(±0.42)		
PC	413.2	(407.9 - 418.7)	5.45	(±0.08)	418.1	(390.8 - 449.6)	5.37	(±0.41)		
OTLC	423.4	(419.9 - 426.9)	6.86	(±0.06)	421.5	(412.9 - 430.5)	6.90	(±0.16)		
PC+OTLC	430.0	(429.8 - 430.2)	6.80	(±0.00)	425.8	(410.6 - 442.2)	6.88	(±0.27)		

FCN period

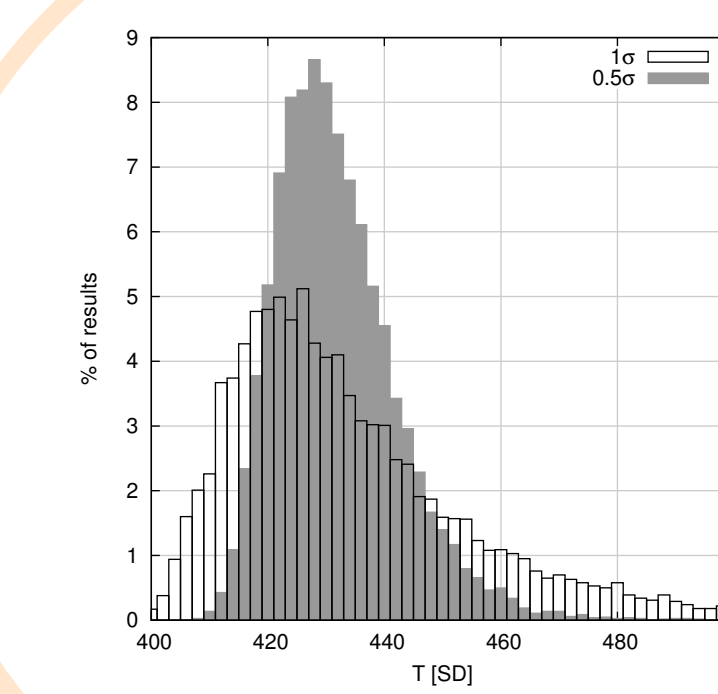


Figure: Monte Carlo simulation of results

Gravity Measurements

Table: Tidal analysis results (diurnal band)

Tide	NC				PC				PC+OTLC			
	f	A	ϕ	σ	f	A	ϕ	σ	f	A	ϕ	σ
O_1	13.99	1.7	13.07	0.007	0.080	1.840	0.008	0.080	13.94	1.840	0.008	0.080
O_2	13.95	0.61	13.04	0.005	0.020	0.600	0.005	0.020	13.94	0.600	0.005	0.020
M_2	14.47	2.17	13.43	0.040	0.200	2.100	0.020	0.200	14.47	2.100	0.020	0.200
M_3	14.50	4.2	13.18	0.018	0.200	3.900	0.020	0.200	14.50	3.900	0.020	0.200
S_2	14.69	1.61	13.67	0.007	0.030	1.580	0.008	0.030	14.69	1.580	0.008	0.030
S_3	14.69	1.1	13.65	0.004	0.020	1.070	0.005	0.020	14.69	1.070	0.005	0.020
K_1	15.01	43.4	13.98	0.002	0.110	43.00	0.003	0.110	15.00	43.00	0.003	0.110
ν_1	15.02	1.3	13.74	0.004	0.230	1.300	0.004	0.230	15.02	1.300	0.004	0.230
ν_2	15.12	4.8	13.74	0.018	0.440	4.700	0.018	0.440	15.12	4.700	0.018	0.440
ν_3	15.00	2.3	13.66	0.008	0.040	2.100	0.008	0.040	15.00	2.100	0.008	0.040
ν_4	15.19	1.8	13.51	0.008	0.360	1.800	0.008	0.360	15.19	1.800	0.008	0.360

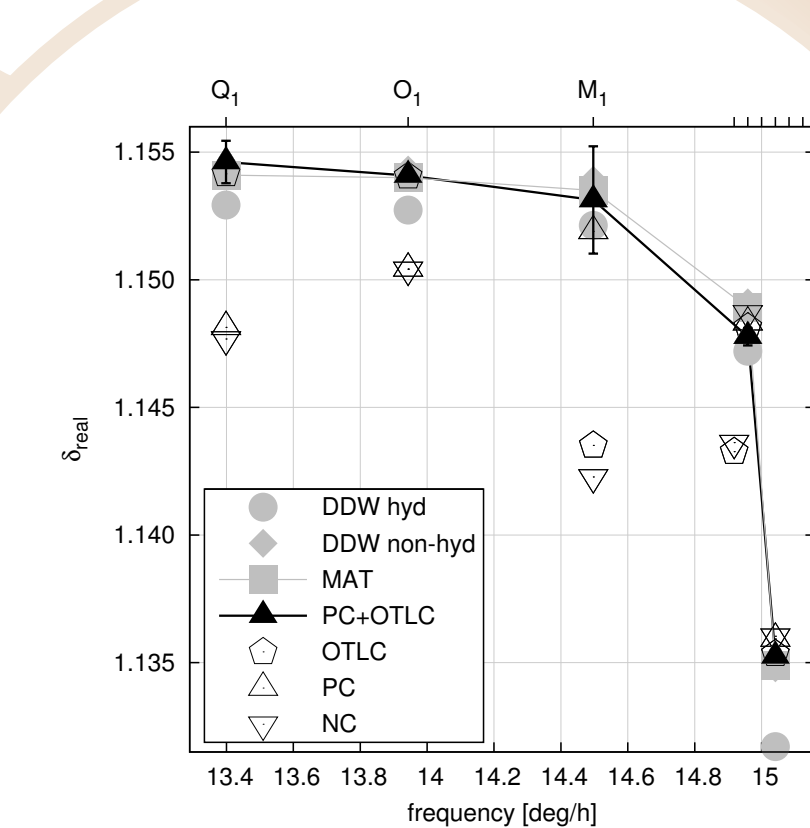


Figure: Comparison of gravimetric factors for diurnal tidal waves. The results when no correction (NC), pressure correction (PC) and ocean tidal loading correction (OTLC) was applied are shown along with theoretical models of Dehant, Defrance, Wahr (DOW) and Matthews (MAT).

Pressure correction (PC) with empirical admittance factor of $-3.5 \text{ nm} \cdot \text{s}^{-2} \cdot \text{hPa}^{-1}$ and ocean tidal loading (OTLC) was performed using most recent ocean models

Józefosław Observatory is located in suburb area of Warsaw
 3.5 years (2007-2010) of continuous gravity measurements with LaCoste&Romberg spring gravimeter

Resonance model

$$\delta(\sigma) = \delta_0 + \frac{\bar{A}}{\sigma - \bar{\sigma}_{NDFW}}$$

$$\delta(\sigma) - \delta(\sigma_0) = \frac{\bar{A}}{\sigma - \bar{\sigma}_{NDFW}} + \frac{\bar{A}}{\sigma_0 - \bar{\sigma}_{NDFW}}$$

$$\sum_{j=1}^n \beta_j \left[\delta(\sigma_j) - \delta(\sigma_0) - \frac{\bar{A}}{\sigma_j - \bar{\sigma}_{NDFW}} + \frac{\bar{A}}{\sigma_0 - \bar{\sigma}_{NDFW}} \right]^2$$

$$\bar{\sigma}_{NDFW} = f(\sigma_1, \sigma_2, \sigma_3, \delta_1, \delta_2, \delta_3)$$

$$\frac{1}{T_{FCN}} = \frac{1}{T_{NDFW}} - 1; \quad Q = \frac{\sigma_{NDFW}^2}{2\sigma_{NDFW}}$$

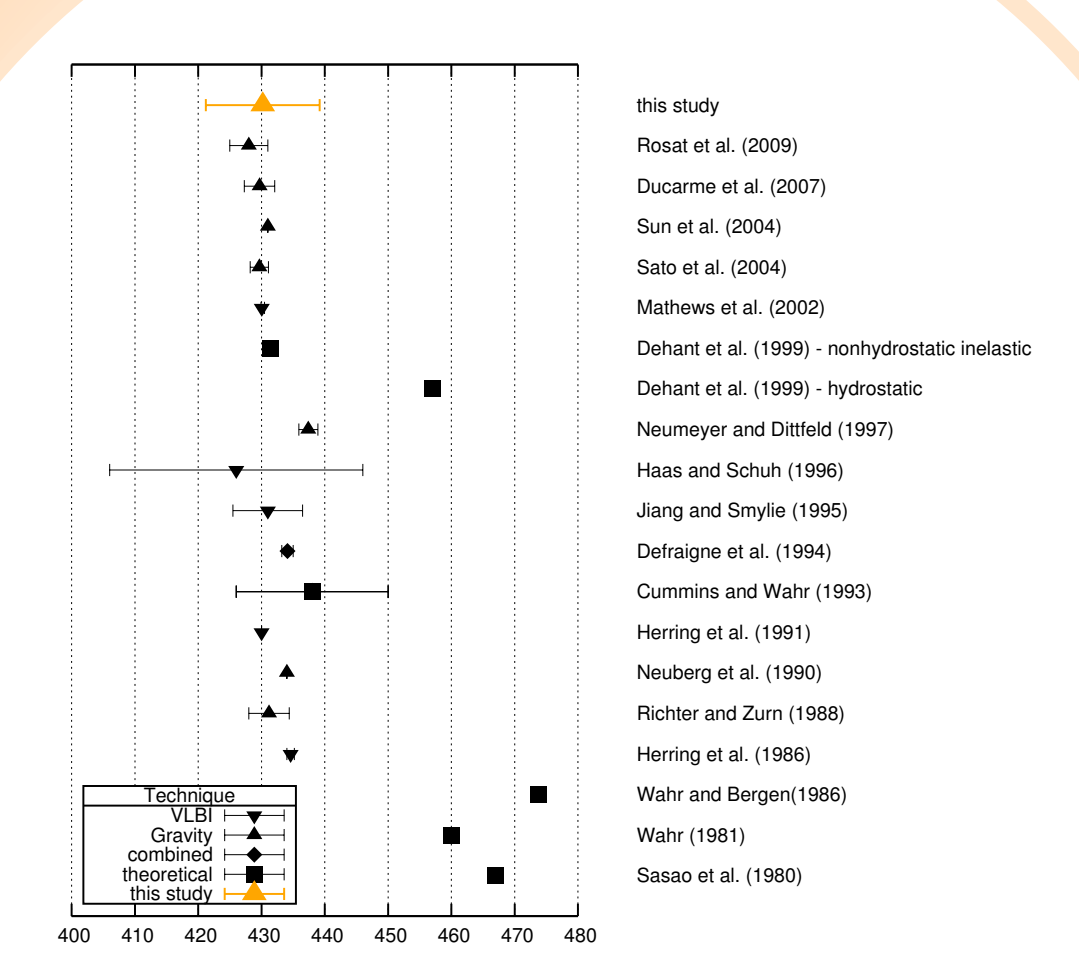


Figure: Comparison of FCN period determination from different studies

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